

Calculus I

Name: \_\_\_\_\_

Study Guide 5

Class: \_\_\_\_\_

Due Date: \_\_\_\_\_

Score: \_\_\_\_\_

No Work  $\Leftrightarrow$  No Points

Use Pencil Only  $\Leftrightarrow$  Be Neat & Organized

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1. (4 points) For any given  $\epsilon > 0$ , find  $\delta > 0$  such that  $\lim_{x \rightarrow 4} \left( \frac{1}{4}x - 1 \right) = 0$ .

1. \_\_\_\_\_

2. (4 points) For any given  $\epsilon > 0$ , find  $\delta > 0$  such that  $\lim_{x \rightarrow -5} (-3x + 2) = 17$ .

2. \_\_\_\_\_

3. (5 points) For any given  $\epsilon > 0$ , find  $0 < \delta \leq 1$  such that  $\lim_{x \rightarrow 1} \sqrt{x} = 1$ .

3. \_\_\_\_\_

4. (4 points) Find  $\lim_{x \rightarrow a} f(x)$  and  $\lim_{x \rightarrow a} g(x)$  if

$$\begin{cases} \lim_{x \rightarrow a} [3f(x) - 2g(x)] = 11 \\ \lim_{x \rightarrow a} [2f(x) + 3g(x)] = 3 \end{cases}$$

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4. \_\_\_\_\_

5. (4 points) Find and simplify the difference quotient for  $f(x) = mx$ , and then evaluate for  $h = 0$ .

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5. \_\_\_\_\_

6. (4 points) Evaluate  $\lim_{x \rightarrow 0} f(x)$  if  $1 - x^2 \leq f(x) \leq \cos x$  for all  $x \in (-\pi/2, \pi/2)$ .

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6. \_\_\_\_\_

7. (4 points) For any given  $\epsilon > 0$ , find  $\delta > 0$  such that  $\lim_{x \rightarrow -3} (|x| - 4) = -1$ .

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7. \_\_\_\_\_

8. (4 points) For any given  $\epsilon > 0$ , find  $\delta > 0$  such that  $\lim_{x \rightarrow 0} \sqrt[5]{x} = 0$ .

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8. \_\_\_\_\_

9. (4 points) For any given  $\epsilon > 0$ , find  $\delta > 0$  such that  $\lim_{x \rightarrow -3} (x^2 + 6x) = -9$ .

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9. \_\_\_\_\_

10. (4 points) Evaluate  $\lim_{x \rightarrow a} \frac{x^4 - a^4}{x^2 - a^2}$ .

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10. \_\_\_\_\_

11. (4 points) Evaluate  $\lim_{x \rightarrow 0} \frac{x}{\sqrt{3 + 2x} - \sqrt{3 - 2x}}$ .

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11. \_\_\_\_\_

12. (5 points) Evaluate  $\lim_{h \rightarrow 0} \frac{f(x + h) - f(x)}{h}$  for  $f(x) = \frac{1}{x}$ .

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12. \_\_\_\_\_